

a) $send(net, A, k_{as}) == out\ net\ A; in\ net\ x; new\ s; out\ net\ \{s, x\}_{k_{as}};$

$Recv(net, k_{bs}) == in\ net\ x; new\ n; out\ net\ n; in\ net\ y; out\ net\ \{x, y\}_{k_{bs}}; in\ net\ z; decrypt\ z\ is\ \{z\}_{k_{bs}}; if\ z \neq spy\ the\ secret\ (z,)$

$Server(net, A, k_{as}, k_{bs}) == in\ net\ x; decrypt\ x\ is\ \{x\}_{k_{bs}}; split\ x\ is\ (y_1, y_2); if\ y_1 = A\ then\ decrypt\ y_2\ is\ z; out\ net\ \{z\}_{k_{bs}};$

$Compromised(k_{spy}) == out\ net\ k_{spy};$

$P(net, A, B, spy) == new\ k_{spy}, k_{as}, k_{bs}; !send(net, A, k_{as}) !send(net, B, k_{bs}) !Recv(net, k_{bs}) !Recv(net, k_{as}) |$
 $!Server(net, A, k_{as}, k_{bs}) !Server(net, B, k_{bs}, k_{as}) !Server(net, A, k_{as}, k_{spy}) !Server(net, B, k_{bs}, k_{spy})$
 $!Server(net, spy, k_{spy}, k_{as}) !Server(net, spy, k_{spy}, k_{bs})$

b) This answer is a bit different from the one in the solutions. The main idea of this answer is to simply pass the challenge from the spy to the server, then have the server present the decrypted secret (which was intended for B) to the spy. However, this solution has one problem: it assumes that the server accepts that the same nonce is seen twice. Strictly speaking, the protocol for the server does not check this. However, if this were to occur in reality, the opponent process below would not work.

$O == in\ net\ k_{spy};$ *get k_{spy} from compromised*
 $in\ net\ n_{BA};$ *get nonce net from B → A*
 $out\ net\ n_{BA};$ *make sure this nonce can still be used by A and B.*
 $in\ net\ s_{n_{k_{as}}};$ *get encrypted message containing s from A*
 $out\ net\ s_{n_{k_{as}}};$ *immediately forward it to B*
 $out\ net\ \{(a, s_{n_{k_{as}}})\}_{k_{spy}};$ *forward challenge to server, but with spy's key*
 $in\ net\ s_{k_{spy}};$ *server answers with {s}_{k_{spy}}*
 $decrypt\ s_{k_{spy}}\ is\ \{s\}_{k_{spy}};$ *decrypt*
 $out\ net\ s;$ *outputs but → s is not secret anymore*

Alternatively, we could consider the following opponent process, which is based on the solutions.

$O == in\ net\ k_{spy};$ *get spy's key*
 $out\ net\ A;$
 $in\ net\ n_A;$ *} create session O(A) → B*
 $out\ net\ spy;$
 $in\ net\ n_{spy};$ *} create session O(spy) → B*
 $new\ f;$ *fake {s_n, n_A} for session O(A) → B*
 $new\ s_{spy};$ *s for O(spy) → B which B will eventually misinterpret as being for O(A) → B*
 $out\ net\ g;$ *have B send {A, g} to S note: B thinks this is the message {A, {s_n, n_A}_{k_{bs}}}
 B will not get a response, due to the message being malformed*
 $out\ net\ \{(s_{spy}, n_A)\}_{k_{spy}};$ *B will forward this message as*
 $\{(spy, \{(s_{spy}, n_A)\}_{k_{spy}})\}_{k_{bs}}$
and receives back
 $\{s_{spy}\}_{k_{bs}}$
*which B misinterprets as the response to {A, {s_n, n_A}_{k_{bs}}}
 and thus, the secret s_{spy} is misinterpreted and shared with A.*
 $out\ net\ s_{spy};$ *O publishes s_{spy}, violating its secrecy*